RESEARCH HIGHLIGHT : DECOMPOSITION NUMBERS FOR SYMMETRIC GROUPS

WORK OF TAN KAI MENG

The complete determination of decomposition numbers for symmetric groups is a longstanding open problem in the modular representation theory of finite groups. These numbers, denoted $d_{\lambda\mu}$, count the multiplicity of the simple module D^{μ} as a composition factor of the Specht module S^{λ} . While a complete solution to this famous problem does not seem forthcoming in the near future, A/P Tan and his co-authors has made significant progress towards such a solution.

In the 1990s, Kleshchev [K] obtained results in the relevant algebraic groups and used them to provide a closed formula, in terms of sign sequences, for $d_{\lambda\mu}$ where the partition μ is obtained from λ by moving one node.

A/P Tan and his undergraduate student Teo Wei Hao extended this [TT] to decomposition numbers $d_{\lambda\mu}$ where μ is obtained from λ by moving any number of nodes, all of which having the same *p*-residue.

Subsequently, with the help of his co-author Joseph Chuang, A/P Tan extended this [CT] even further, to decomposition numbers $d_{\lambda\mu}$ where μ is obtained from λ by moving any number of nodes, all of which having *non-adjacent p*-residues.

References

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