

Research highlight: Flows on the $\mathrm{PGL}(V)$ -Hitchin component

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For a real, finite dimensional vector space V , the $\mathrm{PGL}(V)$ -Hitchin component is a distinguished component of the character variety of representations from a closed surface group to $\mathrm{PGL}(V)$. The representations in these components are known to have very good geometric properties. For example, they are all discrete and faithful [2]. The $\mathrm{PGL}(V)$ -Hitchin component itself is also known to be diffeomorphic to a cell [1], and comes equipped with a natural symplectic structure called the Atiyah-Bott-Goldman symplectic structure.

In this work [3], the authors describe, given an ideal triangulation on the surface, a new way to smoothly deform representations in the $\mathrm{PGL}(V)$ -Hitchin component. These deformations give families of smooth flows on the $\mathrm{PGL}(V)$ -Hitchin component, that they call “parallel flows”. Using these flows, they describe a trivialization of the tangent bundle to the $\mathrm{PGL}(V)$ -Hitchin component. In a companion paper [4], they then show that these parallel flows are all Hamiltonian flows with respect to the Goldman symplectic structure. As a consequence, they find explicit global Darboux coordinates for this symplectic structure.

Reference:

- [1] Nigel Hitchin, Lie groups and Teichmüller space, *Topology* 31 (1992), 449 – 473.
- [2] François Labourie, Anosov flows, surface groups and curves in projective space, *Invent. math.* 165 (2006), 51 – 114.
- [3] Zhe Sun, Anna Wienhard, Tengren Zhang, Flows on the $\mathrm{PGL}(V)$ -Hitchin, *Geom. Funct. Anal.* 30 (2020), 588 – 692.
- [4] Zhe Sun, Tengren Zhang, The Goldman symplectic form on the $\mathrm{PGL}(V)$ -Hitchin component, 2017 preprint, arXiv:1709.03589.